# 6

## **Linear Inequalities**

### **Short Answer Type Questions**

Solve for x, the inequalities in following questions.

**Q.** 
$$1 \frac{4}{x-1} \le 3 \le \frac{6}{x+1} (x > 0)$$

#### **Thinking Process**

First solve the first two inequalities, then solve the last two inequality to get range of x .

**Sol.** Consider first two inequalities,

	$\frac{4}{x+1} \le 3$	
$\Rightarrow$	$4 \le 3(x + 1)$	
$\Rightarrow$	$4 \le 3x + 3$	
$\Rightarrow$	$4-3 \leq 3x$	[subtracting 3 on both sides]
$\Rightarrow$	$1 \le 3x$	
ж.	$x \ge \frac{1}{3}$	(i)

and consider last two inequalities,

	$3 \le \frac{6}{x+1}$	
$\Rightarrow$	$3(x + 1) \le 6$	
$\Rightarrow$	$3x + 3 \le 6$	
$\Rightarrow$	$3x \le 6 - 3$	[subtracting 3 to both sides]
$\Rightarrow$	$\Im x \leq \Im$	[dividing by 3]
.:.	$x \leq 1$	(ii)
From Eqs. (i) and (ii),		
	$x \in \left[\frac{1}{3}, 1\right]$	
	$\frac{1}{3} \le x \le 1$	

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$$Q \cdot 2 \begin{vmatrix} \frac{|x-2|-1}{|x-2|-2} \le 0 \\ \bullet \text{ Thinking Process} \\ \text{First, let } y = |x-2| \text{ and then for the obtained values of y use the property } |x-a| \ge k \Leftrightarrow x \le a - k \text{ or } x \ge a + k \text{ or } x = a + x = a + k \text{ or } x = a + x = a + x = a + x \text{ or } x = a + x =$$

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Q. 4 
$$|x-1| \le 5$$
,  $|x| \ge 2$   
Sol.  
 $|x-1| \le 5$   
 $-5 \le x - 1 \le 5$   
 $-4 \le x \le 6$   
 $x \in [-4, 6]$   
and  
 $|x| \ge 2$   
 $x \le -2 \text{ or } x \ge 2$   
 $\Rightarrow$   
 $x \in (-\infty, -2] \cup [2, \infty)$   
...(ii)

$$x \in (-\infty, -2] \cup [2, \infty) \qquad \dots (ii)$$

On combining Eqs. (i) and (ii), we get

 $x \in (-4, -2] \cup [2, 6]$ 

 $-5 \le \frac{2-3x}{2}$ 

0	<b>5</b> – 5 ≤	2 - 3x	< 9
×.	<b>0</b> – 0 Z	4	<u>&gt;</u> 9

Sol. We have,

	4
$\Rightarrow$	$-20 \le 2 - 3x$
$\Rightarrow$ $\Rightarrow$	$3x \le 2 + 20$
$\Rightarrow$	$3x \leq 22$
$\Rightarrow$	$x \le \frac{22}{3}$
and	$\frac{2-3x}{4} \le 9$
$\Rightarrow$	$2 - 3x \le 36$
$\Rightarrow$	$-3x \le 36 - 2$
$\Rightarrow$	$-3x \le 34$
$\Rightarrow$	$3x \ge -34$
$\begin{array}{c} \Rightarrow \\ \Rightarrow \\ \Rightarrow \\ \Rightarrow \\ \Rightarrow \end{array}$	$x \ge -\frac{34}{3}$
$\Rightarrow$	$-\frac{34}{3} \le x \le \frac{22}{3}$
$\Rightarrow$	$x \in \left[\frac{-34}{3}, \frac{22}{3}\right]$

[multiplying by 4 on both sides]

### **Q.** 6 $4x + 3 \ge 2x + 17$ , 3x - 5 < -2

Sol. We have,	$4x + 3 \ge 2x + 17$	
$\Rightarrow$	$4x - 2x \ge 17 - 3 \Longrightarrow 2x \ge 14$	
$\Rightarrow$	$x \ge \frac{14}{2}$	
$\Rightarrow$	$x \ge 7$	(i)
Also, we have	3x - 5 < -2	
$\Rightarrow$	$3x < -2 + 5 \Longrightarrow 3x < 3$	
$\Rightarrow$	<i>x</i> < 1	(ii)
On combining Eas	(i) and (ii) we see that solution is not possible	hecause nothing is

On combining Eqs. (i) and (ii), we see that solution is not possible because nothing is common between these two solutions. (*i.e.*, x < 1,  $x \ge 7$ ).

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**Q.** 7 A company manufactures cassettes. Its cost and revenue functions are C(x) = 26000 + 30x and R(x) = 43x, respectively, where x is the number of cassettes produced and sold in a week. How many cassettes must be sold by the company to realise some profit?

Sol.	Cost function,	C(x) = 26000 + 30x	
	and revenue function,	R(x) = 43x	
	For profit,	R(x) > C(x)	
	$\Rightarrow$	26000 + 30x < 43x	
	$\Rightarrow$	30x - 43x < -26000	
	$\Rightarrow$	-13x < -26000	
	$\Rightarrow$	13 <i>x</i> > 26000	
	$\Rightarrow$	$x > \frac{26000}{13}$	
	.:.	<i>x</i> > 2000	
	11 0000		

Hence, more than 2000 cassettes must be produced to get profit.

- **Q. 8** The water acidity in a pool is considered normal when the average pH reading of three daily measurements is between 8.2 and 8.5. If the first two pH readings are 8.48 and 8.35, then find the range of pH value for the third reading that will result in the acidity level being normal.
- Sol. Given, first pH value = 8.48and second pH value = 8.35Let third pH value be x. Since, it is given that average pH value lies between 8.2 and 8.5.  $8.2 < \frac{8.48 + 8.35 + x}{3} < 8.5$ *.*..  $8.2 < \frac{16.83 + x}{3} < 8.5$  $\Rightarrow$  $3 \times 8.2 < 16.83 + x < 8.5 \times 3$ ⇒ 24.6 < 16.83 + x < 25.5 $\Rightarrow$ 24.6 - 16.83 < *x* < 25.5 - 16.83  $\Rightarrow$ 7.77 < *x* < 8.67  $\Rightarrow$

Thus, third pH value lies between 7.77 and 8.67.

- Q. 9 A solution of 9% acid is to be diluted by adding 3% acid solution to it. The resulting mixture is to be more than 5% but less than 7% acid. If there is 460 L of the 9% solution, how many litres of 3% solution will have to be added?
- **Sol.** Let *x* L of 3% solution be added to 460 L of 9% solution of acid. Then, total quantity of mixture = (460 + x) L Total acid content in the (460 + x) L of mixture

$$= \left(460 \times \frac{9}{100} + x \times \frac{3}{100}\right)$$

It is given that acid content in the resulting mixture must be more than 5% but less than 7% acid.

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Therefore, 
$$5\% \text{ of } (460 + x) < 460 \times \frac{9}{100} + \frac{3x}{100} < 7\% \text{ of } (460 + x)$$
  

$$\Rightarrow \frac{5}{100} \times (460 + x) < 460 \times \frac{9}{100} + \frac{3}{100}x < \frac{7}{100} \times (460 + x)$$

$$\Rightarrow 5 \times (460 + x) < 460 \times 9 + 3x < 7 \times (460 + x)$$
[multiplying by 100]  

$$\Rightarrow 2300 + 5x < 4140 + 3x < 3220 + 7x$$
Taking first two inequalities,  $2300 + 5x < 4140 + 3x$   

$$\Rightarrow 5x - 3x < 4140 - 2300$$

$$\Rightarrow 2x < 1840$$

$$\Rightarrow x < \frac{1840}{2}$$

$$\Rightarrow x < 920 \dots (i)$$
Taking last two inequalities,  $4140 + 3x < 3220 + 7x$   

$$\Rightarrow 3x - 7x < 3220 - 4140$$

$$\Rightarrow -4x < -920$$

$$\Rightarrow 4x > 920$$

$$\Rightarrow x > 230 \dots (ii)$$
Hence, the number of litres of the 3% solution of acid must be more than 230 L and less than 920 L.

**Q.** 10 A solution is to be kept between 40°C and 45°C. What is the range of temperature in degree fahrenheit, if the conversion formula is  $F = \frac{9}{5}C + 32?$ 

**Sol.** Let the required temperature be 
$$x^{\circ}F$$
.  
Given that,  
 $F = \frac{9}{5}C + 32$   
 $\Rightarrow 5F = 9C + 32 \times 5$   
 $\Rightarrow 9C = 5F - 32 \times 5$   
 $\therefore C = \frac{5F - 160}{9}$   
Since, temperature in degree calcius lies between 40°C to 45°C.  
Therefore,  $40 < \frac{5F - 160}{9} < 45$   
 $\Rightarrow 40 < \frac{5x - 160}{9} < 45$   
 $\Rightarrow 40 < \frac{5x - 160}{9} < 45$   
 $\Rightarrow 40 < 9 < 5x - 160 < 45 \times 9$  [multiplying throughout by 9]  
 $\Rightarrow 360 < 5x - 160 < 405$  [adding 160 throughout]  
 $\Rightarrow 360 + 160 < 5x < 405 + 160$   
 $\Rightarrow 520 < 5x < 565$   
 $\Rightarrow \frac{520}{5} < x < \frac{565}{5}$  [divide throughout by 5]  
 $\Rightarrow 104 < x < 113$   
Hence, the range of temperature in degree fahrenheit is 104 °F to 113°F.

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**Q.** 11 The longest side of a triangle is twice the shortest side and the third side is 2 cm longer than the shortest side. If the perimeter of the triangle is more than 166 cm, then find the minimum length of the shortest side.

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Sol. Let the length of shortest side be x cm.
        According to the given information,
         Longest side = 2 \times Shortest side
                          = 2x \text{ cm}
        and third side = 2 + Shortest side
                         = (2 + x) \,\mathrm{cm}
        Perimeter of triangle = x + 2x + (x + 2) = 4x + 2
        According to the question,
        Perimeter > 166 cm
        \Rightarrow
                                             4x + 2 > 166
        \Rightarrow
                                                 4x > 166 - 2
                                                  4x > 164
        \Rightarrow
                                                  x > \frac{164}{4} = 41 \,\mathrm{cm}
        ....
```

Hence, the minimum length of shortest side be 41cm.

**Q.** 12 In drilling world's deepest hole it was found that the temperature *T* in degree celcius,  $x \mod b$  below the earth's surface was given by  $T = 30 + 25 (x - 3), 3 \le x \le 15$ . At what depth will the temperature be between 155°C and 205°C?

Sol.	Given that,	$T = 30 + 25 (x - 3), \ 3 \le x \le 15$	
	According to the question,		
		155 < <i>T</i> < 205	
	$\Rightarrow$	155 < 30 + 25 (x - 3) < 205	
	$\Rightarrow$	155 - 30 < 25 (x - 3) < 205 - 30	[subtracting 30 in whole]
	$\Rightarrow$	125 < 25 (x - 3) < 175	
	$\Rightarrow$	$\frac{125}{25} < x - 3 < \frac{175}{25}$	[dividing by 25 in whole]
	$\Rightarrow$	5< <i>x</i> - 3< 7	
	$\Rightarrow$	5 + 3 < x < 7 + 3	[adding 3 in whole]
	$\Rightarrow$	8 <i>&lt; x &lt;</i> 10	

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Hence, at the depth 8 to10 km temperature lies between 155° to 205°C.

### Long Answer Type Questions

**Q.13** Solve the following system of inequalities 
$$\frac{2x+1}{7x-1} > 5$$
,  $\frac{x+7}{x-8} > 2$ .

**Sol.** The given system of inequations is  $\frac{2x + 7x}{7x - 7x}$ 

...(ii)

and Now,

 $\Rightarrow$ 

 $\Rightarrow$ 

 $\Rightarrow$ 

 $\Rightarrow$ 

 $\frac{\frac{x+7}{x-8} > 2}{\frac{2x+1}{7x-1} - 5 > 0}$   $\frac{\frac{(2x+1)-5(7x-1)}{7x-1} > 0}{\frac{2x+1-35x+5}{7x-1} > 0}$   $\frac{\frac{2x+1-35x+5}{7x-1} > 0 \Rightarrow \frac{33x-6}{7x-1} < 0$   $x \in \left(\frac{1}{7}, \frac{6}{33}\right) \qquad \dots (iii)$   $\downarrow \rightarrow + -\frac{1}{-1/7} = \frac{1}{6/33} + \frac{1}{+\infty}$ 

and  

$$\frac{x+7}{x-8} > 2 \Rightarrow \frac{x+7}{x-8} - 2 > 0$$

$$\Rightarrow \qquad \frac{x+7-2(x-8)}{x-8} > 0 \Rightarrow \frac{x+7-2x+16}{x-8} > 0$$

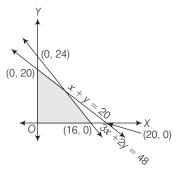
$$\Rightarrow \qquad \frac{-x+23}{x-8} > 0 \Rightarrow \frac{x-23}{x-8} < 0$$

$$\xrightarrow{-\infty + 8} -23 + +\infty$$

$$\Rightarrow \qquad x \in (8, 23)$$

Since, the intersection of Eqs. (iii) and (iv) is the null set. Hence, the given system of equation has no solution.

**Q.14** Find the linear inequalities for which the shaded region in the given figure is the solution set.



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...(iv)

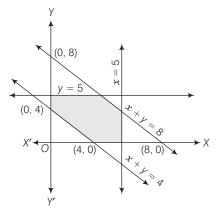
**Sol.** Consider the line 3x + 2y = 48, we observe that the shaded region and the origin are on the same side of the line 3x + 2y = 48 and (0, 0) satisfy the linear constraint  $3x + 2y \le 48$ . So, we must have one inequation as  $3x + 2y \le 48$ .

Now, consider the line x + y = 20. We find that the shaded region and the origin are on the same side of the line x + y = 20 and (0, 0) satisfy the constraints  $x + y \le 20$ . So, the second inequation is  $x + y \le 20$ .

We also notice that the shaded region is above X-axis and is on the right side of Y-axis, so we must have  $x \ge 0$ ,  $y \ge 0$ .

Thus, the linear inequations corresponding to the given solution set are  $3x + 2y \le 48$ ,  $x + y \le 20$  and  $x \ge 0$ ,  $y \ge 0$ .

**Q.** 15 Find the linear inequalities for which the shaded region in the given figure is the solution set.



**Sol.** Consider the line x + y = 4.

We observe that the shaded region and the origin lie on the opposite side of this line and (0, 0) satisfies  $x + y \le 4$ . Therefore, we must have  $x + y \ge 4$  as the linear inequation corresponding to the line x + y = 4.

Consider the line x + y = 8, clearly the shaded region and origin lie on the same side of this line and (0, 0) satisfies the constraints  $x + y \le 8$ . Therefore, we must have  $x + y \le 8$ , as the linear inequation corresponding to the line x + y = 8.

Consider the line x = 5. It is clear from the graph that the shaded region and origin are on the left of this line and (0, 0) satisfy the constraint  $x \le 5$ .

Hence,  $x \le 5$  is the linear inequation corresponding to x = 5.

Consider the line y = 5, clearly the shaded region and origin are on the same side (below) of the line and (0, 0) satisfy the constrain  $y \le 5$ .

Therefore,  $y \le 5$  is an inequation corresponding to the line y = 5.

We also notice that the shaded region is above the X-axis and on the right of the Y-axis *i.e.*, shaded region is in first quadrant. So, we must have  $x \ge 0$ ,  $y \ge 0$ .

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Thus, the linear inequations comprising the given solution set are

 $x + y \ge 4$ ;  $x + y \le 8$ ;  $x \le 5$ ;  $y \le 5$ ;  $x \ge 0$  and  $y \ge 0$ .

### **Q.16** Show that the following system of linear inequalities has no solution $x+2y \le 3, 3x+4y \ge 12, x \ge 0, y \ge 1.$

**Sol.** Consider the inequation  $x + 2y \le 3$  as an equation, we have

x + 2y = 3
r = 3 - 2v

 $\Rightarrow$  $\Rightarrow$ 

$\begin{array}{c} x - 3 - 2y \\ 2y = 3 - x \end{array}$				
<b>x</b> 3 1 0				
у	0	1	1.5	

Now, (0, 0) satisfy the inequation  $x + 2y \le 3$ .

So, half plane contains (0, 0) as the solution and the line x + 2y = 3 intersect the coordinate axis at (3, 0) and (0, 3/2).

Consider the inequation  $3x + 4y \ge 12$  as an equation, we have 3x + 4y = 12 $\Rightarrow \qquad 4y = 12 - 3x$ 

x	0	4	2
у	3	0	3/2

Thus, coordinate axis intersected by the line 3x + 4y = 12 at points (4, 0) and (0, 3).

Now, (0, 0) does not satisfy the inequation 3x + 4y = 12.

Therefore, half plane of the solution does not contained (0, 0).

Consider the inequation  $y \ge 1$  as an equation, we have

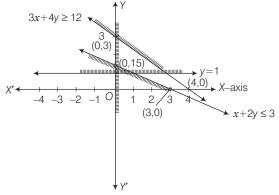
It represents a straight line parallel to X-axis passing through point (0, 1).

Now, (0, 0) does not satisfy the inequation  $y \ge 1$ .

Therefore, half plane of the solution does not contains (0, 0).

Clearly  $x \ge 0$  represents the region lying on the right side of Y-axis.

The solution set of the given linear constraints will be the intersection of the above region.



It is clear from the graph the shaded portions do not have common region. So, solution set is null set.

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### **Q.17** Solve the following system of linear inequalities $3x + 2y \ge 24$ , $3x + y \le 15$ , $x \ge 4$ .

**Sol.** Consider the inequation  $3x + 2y \ge 24$  as an equation, we have 3x + 2y = 24.  $\Rightarrow \qquad 2y = 24 - 3x$ 

x	0	8	4
у	12	0	6

Hence, line 3x + y = 24 intersect coordinate axes at points (8, 0) and (0,12). Now, (0,0) does not satisfy the inequation  $3x + 2y \ge 24$ . Therefore, half plane of the solution set does not contains (0,0). Consider the inequation  $3x + y \le 15$  as an equation, we have

⇒

3x + y = 15 $y = 15 - 3x$				
x	0	5	3	
у	15	0	6	

Line 3x + y = 15 intersects coordinate axes at points (5,0) and (0,15).

Now, point (0,0) satisfy the inequation  $3x + y \le 15$ .

Therefore, the half plane of the solution contain origin.

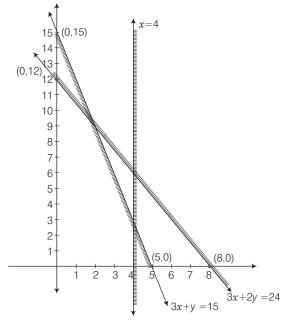
Consider the inequality  $x \ge 4$  as an equation, we have

$$x = 4$$

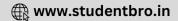
It represents a straight line parallel to Y -axis passing through (4,0). Now, point (0,0) does not satisfy the inequation  $x \ge 4$ .

Therefore, half plane does not contains (0,0),

The graph of the above inequations is given below.



It is clear from the graph that there is no common region corresponding to these inequality. Hence, the given system of inequalities have no solution.



### **Q.18** Show that the solution set of the following system of linear inequalities is an unbounded region $2x + y \ge 8$ , $x + 2y \ge 10$ , $x \ge 0$ , $y \ge 0$ .

 $\Rightarrow$ 

 $\Rightarrow$ 

2x +	<i>y</i> = 8
	y = 8 - 2x

x	0	4	3
y	8	0	2

The line 2x + y = 8 intersects coordinate axes at (4,0) and (0, 8). Now, point (0,0) does not satisfy the inequation  $2x + y \ge 8$ . Therefore, half plane does not contain origin.

Consider the inequation  $x + 2y \ge 10$ , as an equation, we have

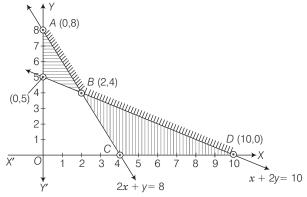
x + 2y = 10 $2y = 10 - x$				
x	10	0	8	
у	0	5	1	

The line 2x + y = 8 intersects the coordinate axes at (10,0) and (0,5).

Now, point (0,0) does not satisfy the inequation  $x + 2y \ge 10$ .

Therefore, half plane does not contain (0,0).

Consider the inequation  $x \ge 0$  and  $y \ge 0$  clearly, it represents the region in first quadrant. The graph of the above inequations is given below



It is clear from the graph that common shaded portion is unbounded.

### **Objective Type Questions**

**O.** 19 If *x* < 5, then (a) -x < -5(b)  $-x \le -5$ (c) -x > -5(d)  $-x \ge -5$ **Sol.** (c) If x < 5, then -x > -5[if we multiply by negative numbers, then inequality get reversed] **Q.** 20 If x, y and b are real numbers and x < y, b < 0, then (a)  $\frac{x}{b} < \frac{y}{b}$  (b)  $\frac{x}{b} \le \frac{y}{b}$  (c)  $\frac{x}{b} > \frac{y}{b}$  (d)  $\frac{x}{b} \ge \frac{y}{b}$ x < y, b < 0Sol. (c) It is given that,  $\frac{x}{b} > \frac{y}{b}$ [∵ *b* < 0]  $\Rightarrow$ **Q.** 21 If -3x + 17 < -13, then (a)  $x \in (10, \infty)$  (b)  $x \in [10, \infty)$  (c)  $x \in (-\infty, 10]$  (d)  $x \in [-10, 10)$ **Sol.** (*a*) Given that, -3x + 17 < -133x - 17 > 13[multiplying by -1 on both sides]  $\Rightarrow$  $\Rightarrow$ 3x > 13 + 17[adding 17 on both sides] 3x > 30 $\Rightarrow$ *x* > 10 *.*.. **Q.** 22 If x is a real number and |x| < 3, then (b) -3 < x < 3(a)  $x \ge 3$ (c)  $x \le -3$ (d)  $-3 \le x \le 3$ Sol. (b) Given, | *x* | < 3 -3 < x < 3 $[::|x| < a \Rightarrow -a < x < a]$  $\Rightarrow$ **Q.** 23 Let x and b are real numbers. If b > 0 and |x| > b, then (a)  $x \in (-b, \infty)$ (b)  $x \in [-\infty, b)$ (d)  $x \in (-\infty, -b) \cup (b, \infty)$ (c)  $x \in (-b, b)$ Sol. (d) Given, |x| > b and b > 0x < -b or x > b $\Rightarrow$  $x \in (-\infty, -b) \cup (b, \infty)$  $\Rightarrow$ **Q.** 24 If |x - 1| > 5, then (a)  $x \in (-4, 6)$ (b)  $x \in [-4, 6]$ (c)  $x \in (-\infty, -4) \cup (6, \infty)$ (d)  $x \in [-\infty, -4) \cup [6, \infty)$ Sol. (c) Given, |x-1| > 5(x-1) < -5 or (x-1) > 5 $[\because |x| > a \Rightarrow x < a \text{ or } x > a]$  $\Rightarrow$ x < -4 or x > 6 $\Rightarrow$  $\Rightarrow$  $x \in (-\infty, -4) \cup (6, \infty)$ 

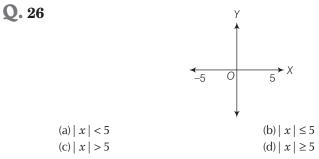
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**Q.** 25 If  $|x+2| \le 9$ , then (a)  $x \in (-7, 11)$ (b)  $x \in [-11, 7]$ (c)  $x \in (-\infty, -7) \cup (11, \infty)$ (d)  $x \in (-\infty, -7) \cup [11, \infty)$ Sol. (b) Given,  $|x+2| \le 9$ ,  $[::| x | \le a \Rightarrow -a \le x \le a]$  $\Rightarrow$  $-9 \le x + 2 \le 9$  $\Rightarrow$  $-9 - 2 \le x \le 9 - 2$ [subtracting 2 througout]  $-11 \le x \le 7$  $\Rightarrow$  $\Rightarrow$  $x \in [-11,7]$ 

The inequality representing the following graphs is



**Sol.** (*a*) The given graph represent x > -5 and x < 5.

On combining these two result, we get

Solution of a linear inequality in variable x is represented on number line in following questions.

**Q**. 27

	-	5	$\rightarrow$
(a) $x \in (-\infty, 5)$		5	(b) $x \in (-\infty, 5]$
(c) $x \in [5, \infty)$			(d) $x \in (5, \infty)$

**Sol.** (d) The given graph represents all the values greater than 5 except x = 5 on the real line So,  $x \in (5, \infty)$ .

### **Q.** 28

(a) 
$$x \in \left(\frac{9}{2}, \infty\right)$$
  
(b)  $x \in \left[\frac{9}{2}, \infty\right)$   
(c)  $x \in -\left[\infty, \frac{9}{2}\right]$   
(d)  $x \in \left(-\infty, \frac{9}{2}\right]$ 

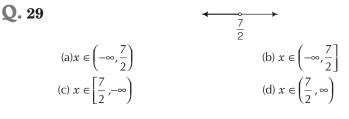
**Sol.** (b) The given graph represents all the values greater than  $\frac{9}{2}$  including  $\frac{9}{2}$  as the real line.

$$x \in \left[\frac{9}{2}, \infty\right)$$

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**Sol.** (*a*) The given graph represents all the values less than  $\frac{7}{2}$  on the real line.

$$\Rightarrow \qquad \qquad x \in \left(-\infty, \frac{7}{2}\right)$$

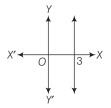
<b>Q.</b> 30		<b>←</b> _2	$\rightarrow$
	$= (-\infty, -2)$ $= (-2, \infty]$		(b) $x \in (-\infty, -2]$ (d) $x \in [-2, \infty)$

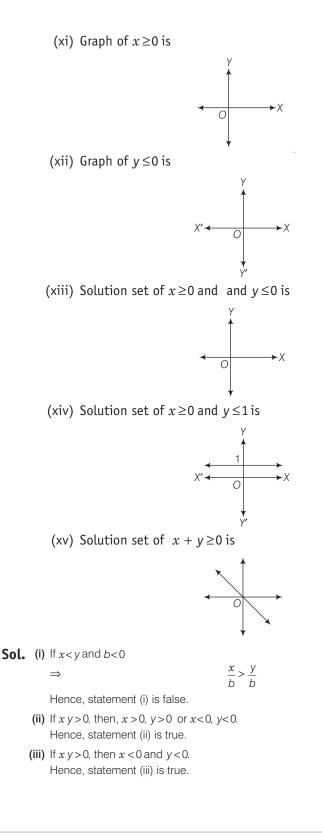
**Sol.** (b) The given graph represents all values less than -2 including -2.  $\Rightarrow \qquad x \in (-\infty, -2]$ 

### **True/False**

**Q. 31** State which of the following statements is true of false.

- (i) If x < y and b < 0, then  $\frac{x}{b} < \frac{y}{b}$ .
- (ii) If xy > 0, then x > 0 and y < 0
- (iii) If xy > 0, then x < 0 and y < 0
- (iv) If xy < 0, then x < 0 and y < 0
- (v) If x < -5 and x < -2, then  $x \in (-\infty, -5)$
- (vi) If x < -5 and x > 2, then  $x \in (-5, 2)$
- (vii) If x > -2 and x < 9, then  $x \in (-2, 9)$
- (viii) If |x| > 5, then  $x \in (-\infty, -5) \cup [5, \infty)$ 
  - (ix) If  $|x| \le 4$ , then  $x \in [-4, 4]$
  - (x) Graph of x < 3 is





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- (iv) If  $xy < 0 \Rightarrow x < 0$ , y > 0 or x > 0, y < 0. Hence, statement (iv) is false.
- (v) If x < -5 and x < -2, then  $x \in (-\infty, -5)$ Hence, statement (v) is true.
- (vi) If x < -5 and x > 2, then x have no value. Hence, statement (vi) is false.
- (vii) If x > -2 and x < 9, then  $x \in (-2, 9)$ . Hence, statement (vii)is true.
- (viii) If |x| > 5, then either x < -5 or x > 5.  $\Rightarrow \qquad x \in (-\infty, -5) \cup (5, \infty)$ Hence, statement (viii) is false.
- (ix) If  $|x| \leq 4$ , then

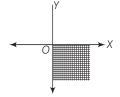
 $\Rightarrow$ 

$$-4 \le x \le 4$$

$$x \in [-4, 4]$$

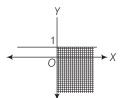
Hence, statement (ix) is true.

- (x) The given graph represents  $x \le 3$ . Hence, statement (x) is false.
- (xi) The given graph represents  $x \ge 0$ . Hence, statement (xi) is true.
- (xii) The given graph represent  $y \ge 0$ . Hence, statement (xii) is false.
- (xiii) Solution set of  $x \ge 0$  and  $y \le 0$  is



Hence, statement (xiii) is false.

(xiv) Solution set of  $x \ge 0$  and  $y \le 1$  is



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Hence, statement (xiv) is false.

(xv) The given graph represents  $x + y \ge 0$ . Hence, statement (xv) is correct.

### Fillers

**Q. 32** Fill in the blanks of the following (i) If  $-4x \ge 12$ , then  $x \dots -3$ . (ii) If  $\frac{-3}{4}x \le -3$ , then *x*...4. (iii) If  $\frac{2}{x+2} > 0$ , then *x*...-2. (iv) If x > -5, then 4x...-20. (v) If x > y and z < 0, then  $-xz \dots -yz$ . (vi) If p > 0 and q < 0, then  $p - q \dots p$ . (vii) If |x + 2| > 5, then x...-7 or x...3. (viii) If  $-2x+1 \ge 9$ , then *x*...-4. **Sol.** (i) If  $-4x \ge 12 \Rightarrow x \le -3$ (ii) If  $\frac{-3}{4} x \le -3$  $x \ge (-3) \times \frac{4}{-3} \Rightarrow x \ge 4$  $\Rightarrow$ (iii) If  $\frac{2}{x+2} > 0$ - -2 + x > -2 $\Rightarrow$ (iv) If  $x > -5 \Rightarrow 4x > -20$ (v) If x > y and z < 0, then [since, z < 0] x Z < VZ $\Rightarrow$ -xZ > -YZ(vi) If p>0 and q<0, then p - q > pe.g., consider 2 > 0 and -3 < 0. 2 - (-3) = 2 + 3 = 5 > 2 $\Rightarrow$ (vii) If |x + 2| > 5, then x + 2 < -5 or x + 2 > 5x < -5 - 2 or x > 5 - 2 $\Rightarrow$ x < -7 or x > 3 $\Rightarrow$  $x \in (-\infty, -7) \cup (3, \infty)$  $\Rightarrow$ (viii) If  $-2x + 1 \ge 9$ , then  $-2x \ge 9 - 1 \implies -2x \ge 8$  $2x \leq -8 \implies x \leq -4$  $\Rightarrow$ 

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